

# Linear-time CSG Rendering of Intersected Convex Objects

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## Graphics Hardware Trends

- Faster polygon rasterisation
- Higher bandwidth
- Larger amounts of memory
- Pipeline Parallelisation & Graphics Clustering

*Objective:* Hardware-based algorithms for CSG rendering.

*Context:* Dynamic and interactive applications.

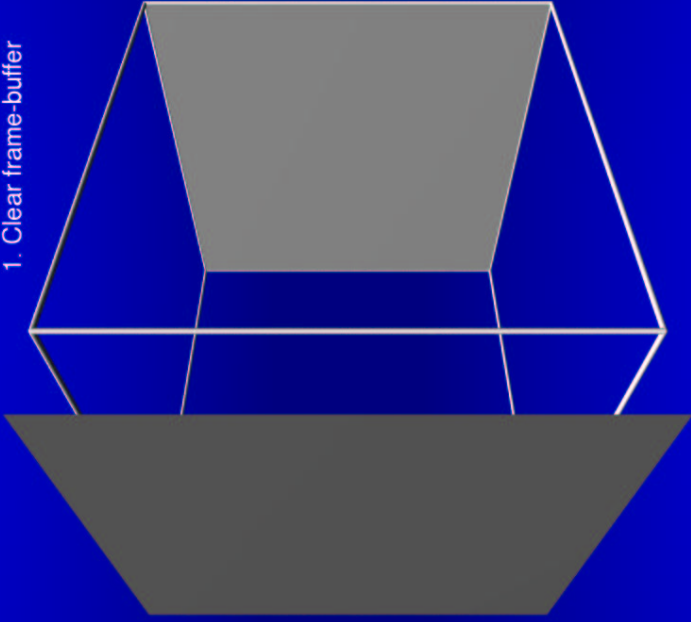
## Overview

- Graphics Hardware Trends
- Z-Buffer
- Z-Buffer Intersection
- SCS CSG Algorithm
- Performance
- Conclusion & Future Work
- Live Demo
- MPEG Movies

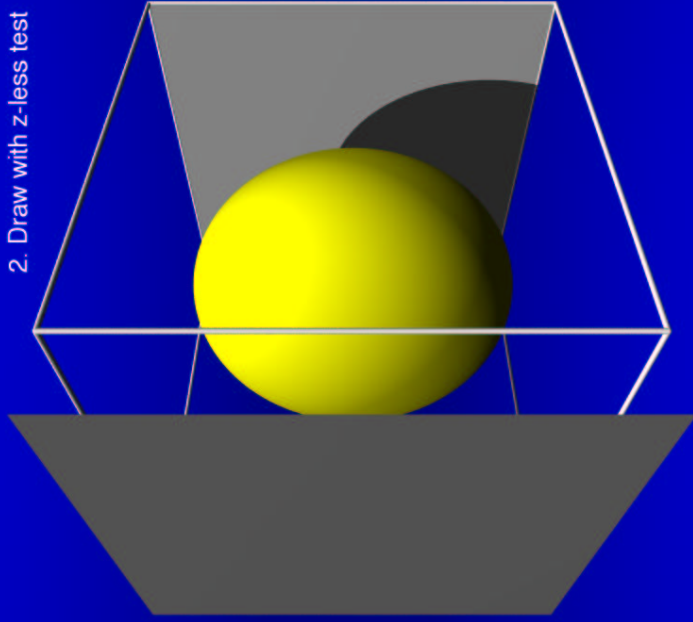
## Z-Buffer

- Hardware-based solution to visible-surface problem.
  - Implied volumetric union.
  - Store z for each pixel in graphics hardware.
  - Configurable z-test as part of pipeline.
1. Initialise the z-buffer to  $Z_{far}$
  2. Only draw pixels closer than z-buffer.
  3. Update z-buffer when z-test passes.

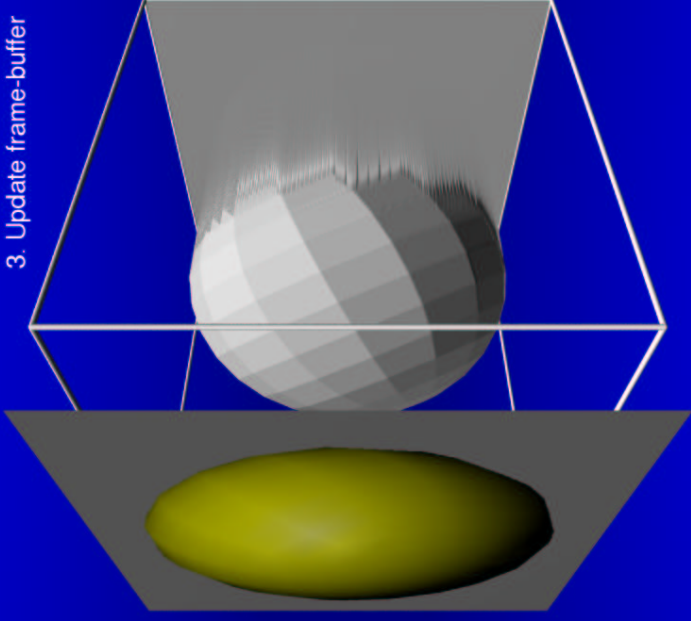
1. Clear frame-buffer



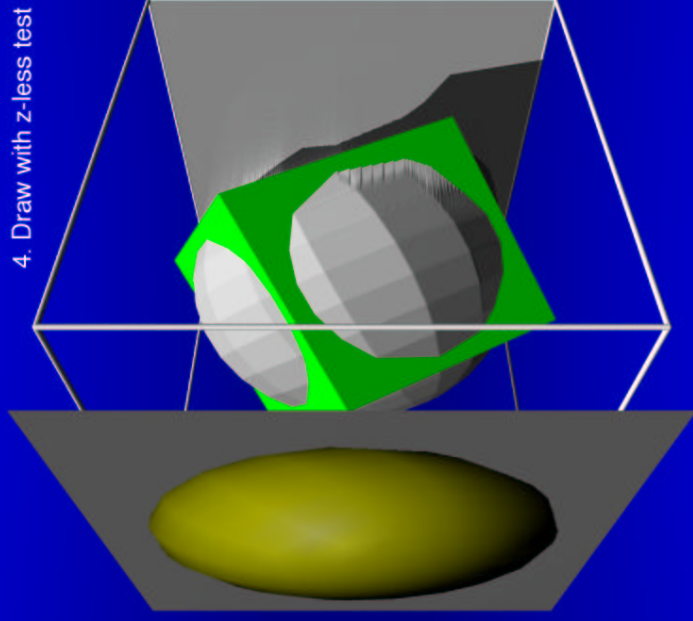
2. Draw with z-less test

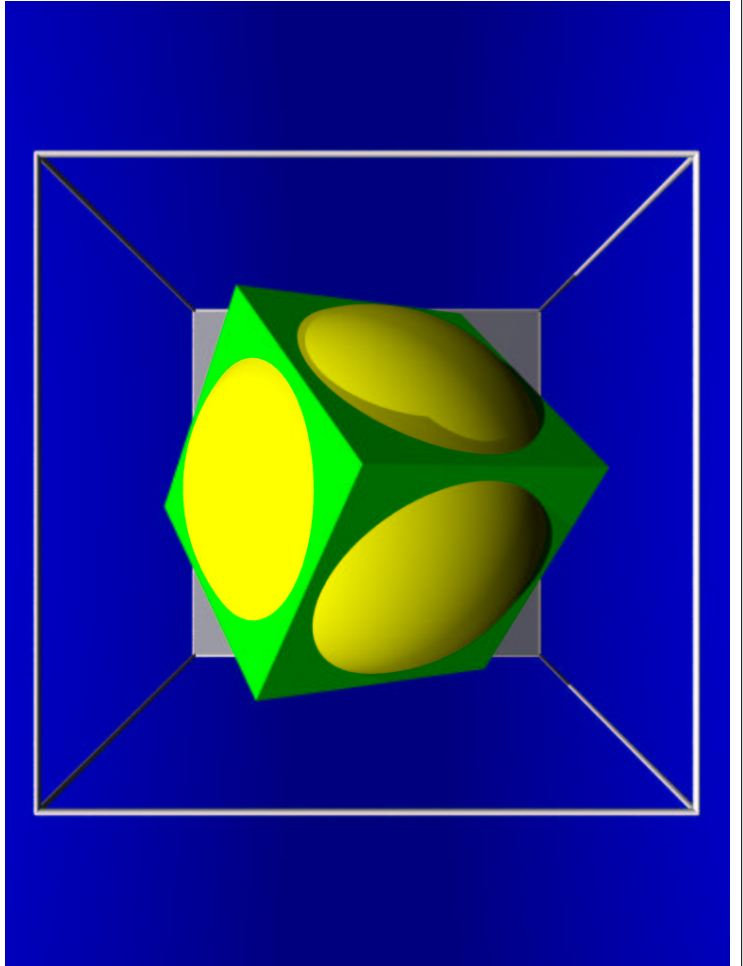
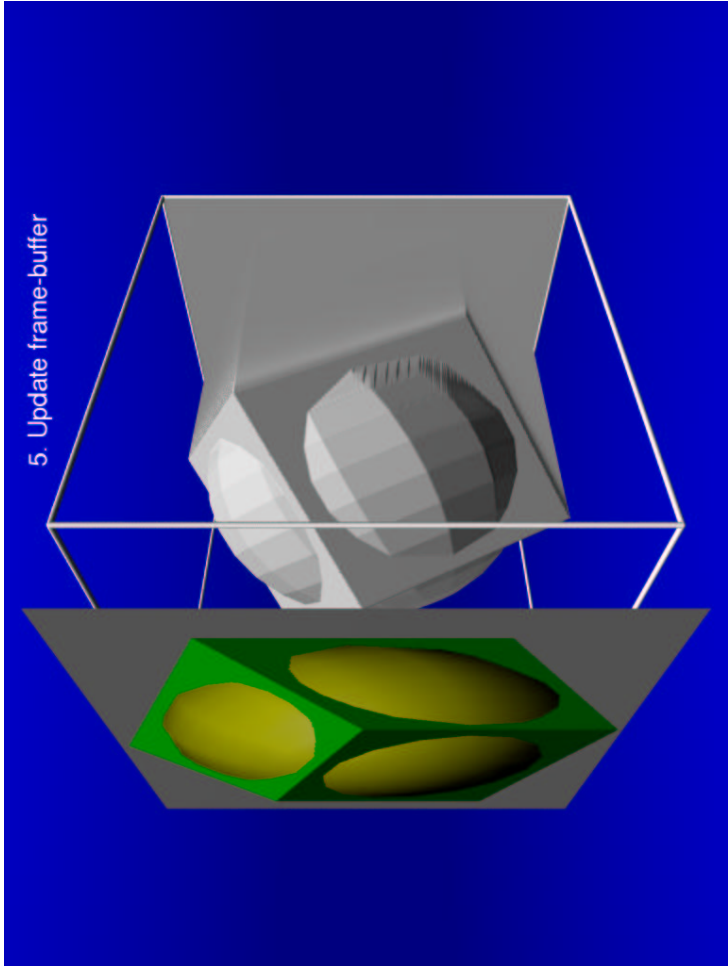
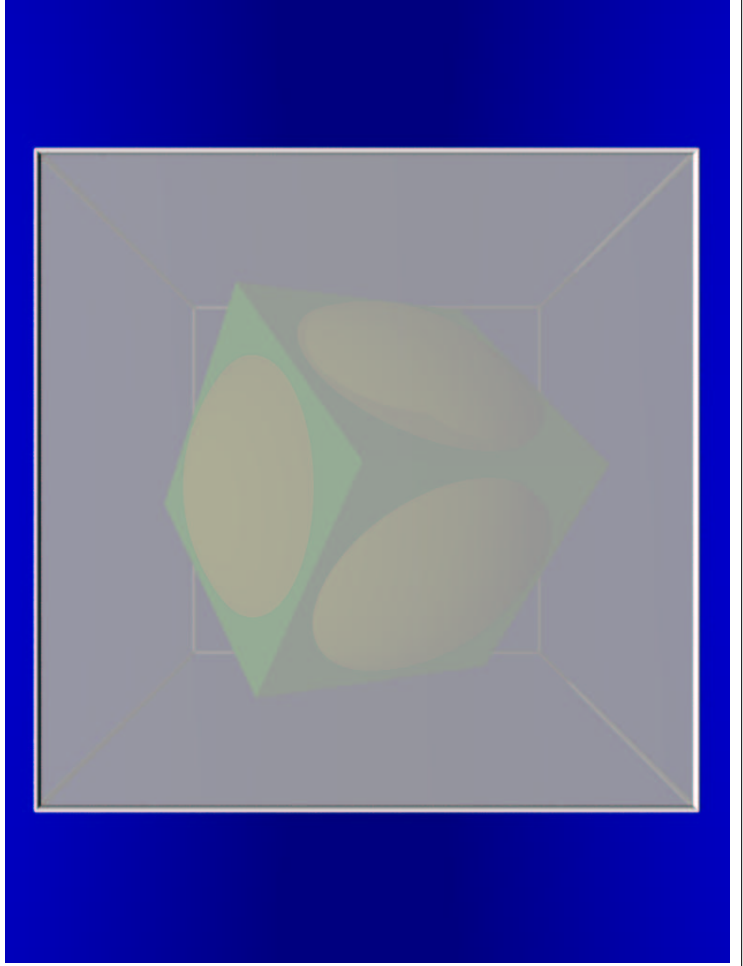
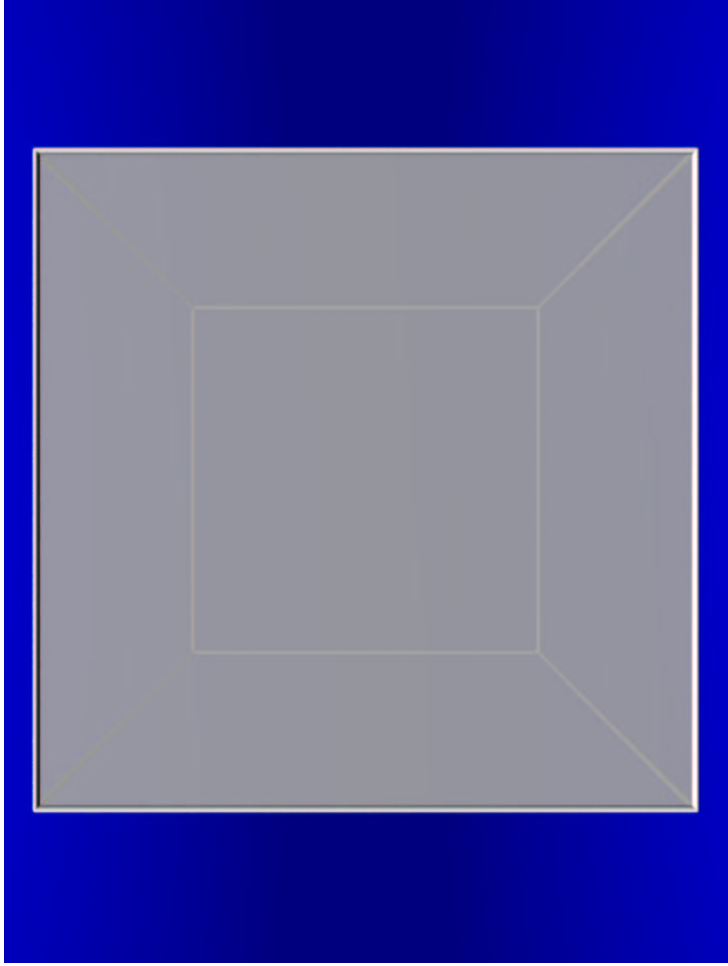


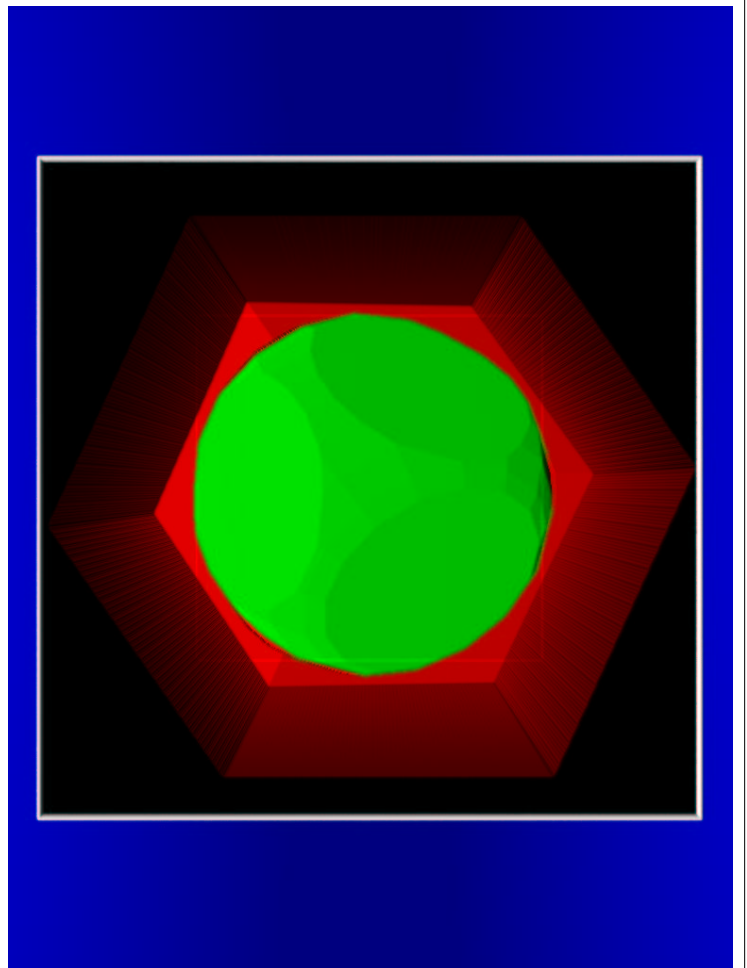
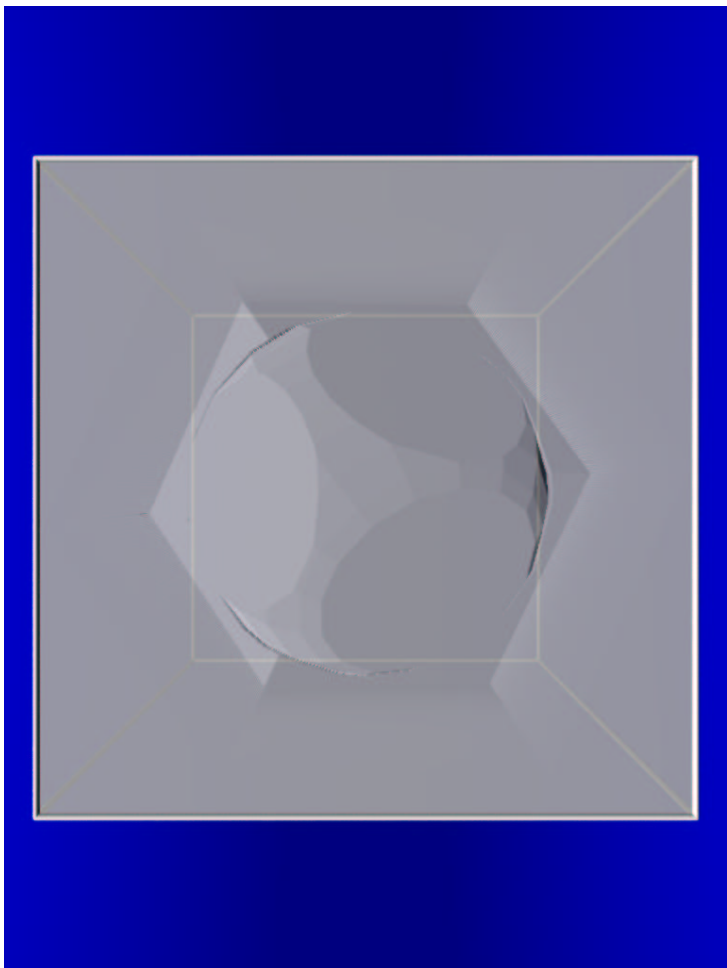
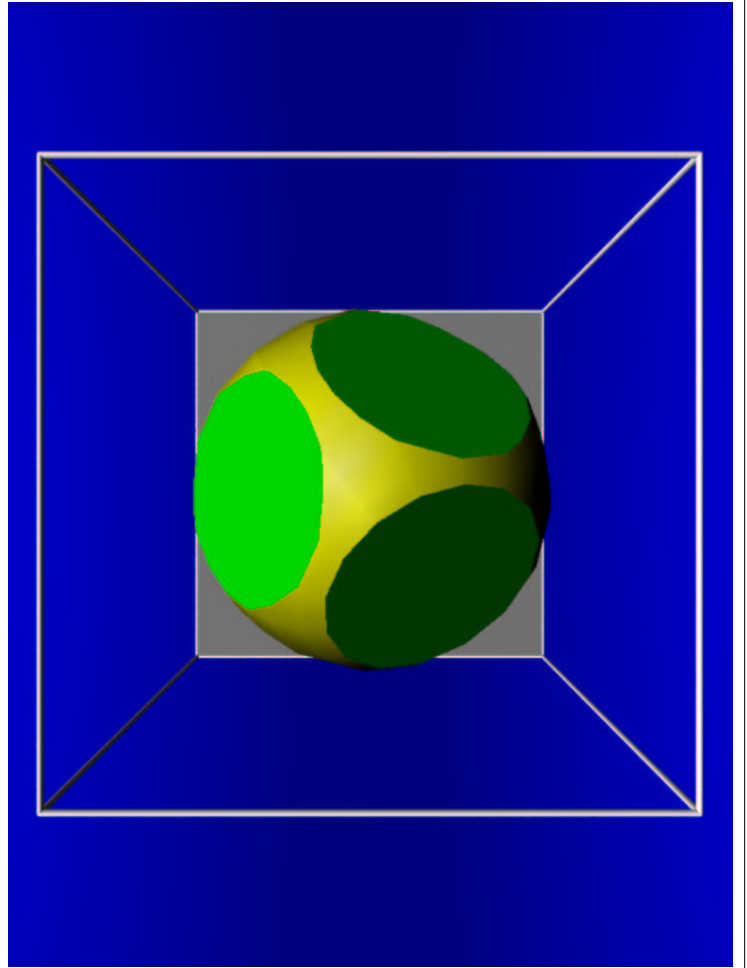
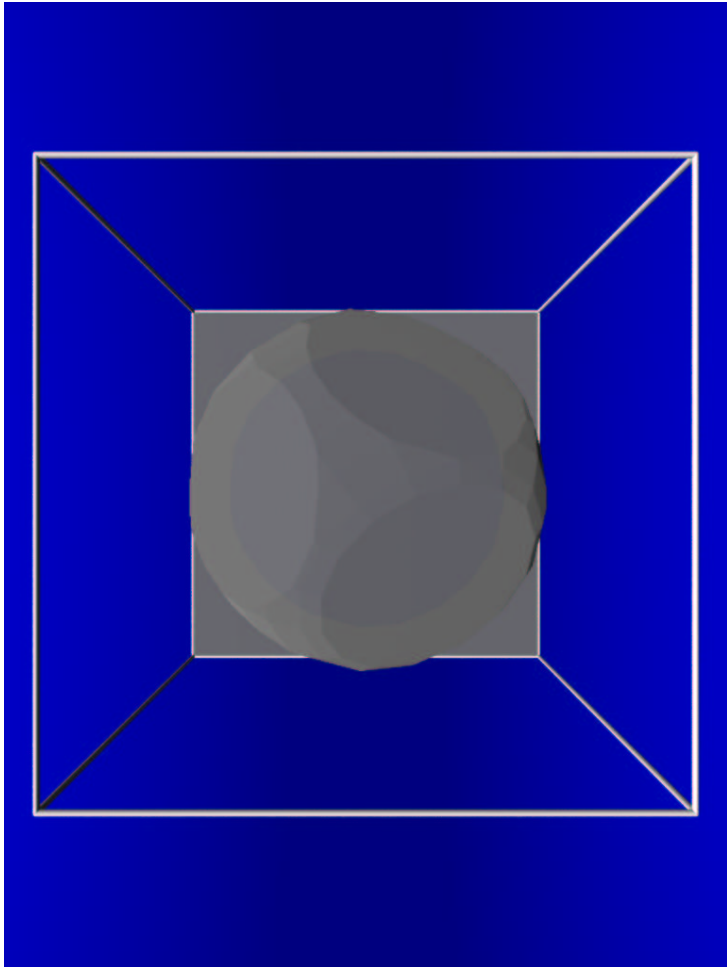
3. Update frame-buffer



4. Draw with z-less test



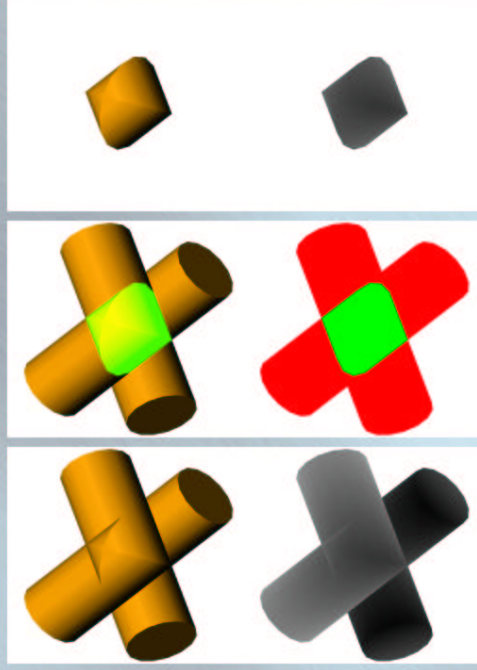




## Z-Buffer Intersection

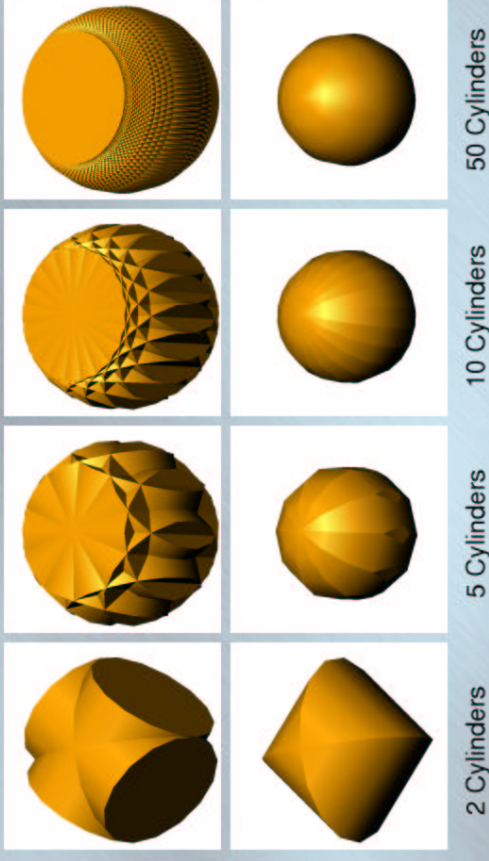
- Algorithm for rendering the intersection of convex objects.
  - Use the z-buffer and stencil buffer.
1. Initialise the z-buffer to  $Z_{near}$
  2. Draw front-facing surfaces with *z-greater* test
  3. Count back-facing surfaces behind z-buffer
  4. Reset pixels where *stencil*  $\neq n$
  5. Draw front-facing surfaces with z-equal test

## SCS-Intersection Illustration



Furthest front-face    Count back-facing behind    Reset pixels

## SCS-Intersection Results



## SCS CSG Algorithm

Algorithm for rendering CSG trees of convex objects.

1. Convert CSG tree to sum-of-products
2. For each product:
  - 2.1 Resolve intersections in z-buffer
  - 2.2 Resolve subtractions in z-buffer
  - 2.3 Merge z-buffer with accumulated result
3. Draw visible surfaces with *z-equal* test

## Performance

- Convex intersection resolved in  $O(n)$  time.
- Convex subtraction still requires  $O(n^2)$  time.
- Speedup depends on relative number of intersections and subtractions.
- Z-buffer copying still a major bottleneck for multiple CSG products.

## Future Work

- Improve performance for convex subtraction.
- Real-world applications: 5-axis NC verification.
- Models for deeper frame buffers in OpenGL 2.0

## Conclusion

- Convex Intersection rendered in linear time on standard OpenGL graphics hardware.
- SCS-Intersect utilised by SCS algorithm for general CSG rendering.
- Interactive frame rates on consumer-grade graphics hardware.